# Control of a Six-axis Robotic Arm Using the Touch Panel 

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#### Abstract

The touch panel used for this experiment is the WEINTECH MT6071iE. The six-axis robotic arm was controlled by an AT90CAN128, manufactured by the ATMEL Company. A DGServo servomotor was used to drive the robots joints, which consisted of four servomotors with 12 kg torque, two 1.8 kg servomotors with reduction gear, and some precision aluminum alloy components. Driven by the servomotors, the robotic arm was able to perform motions like fetching, pinching, catching, and releasing. For example, the robotic arm was able to clamp table tennis balls and carry coke cans. In this paper, the $\mathrm{D}-\mathrm{H}$ method is adopted to set the relative position coordinates of all the joints and connecting rods of the robot arm, and the terminal coordinates of the robotic arm were deduced by combining the degree of freedom with the mechanical limitation of existing arms in accordance with forward kinematics. The results of the D-H method derivation and the actual control results of the robotic arm were compared and the source of error was discussed.


Keywords: Touch panel, Six-axis robotic arm, Servo motor, D-H method, Forward kinematic

## 1 Introduction

The definition of an industrial robot given by the International Federation of Robotics is that it can be reprogrammed, equipped with multi-function robotic arms [1-5], and is able to carry material, parts, tools, or other special devices by performing various designed motions [6-7]. Industrial robots are mainly utilized in various manufacturing plants. They perform functions, such as panel and wafer welding, assembling, carrying, and packaging. Robotic arms are the form an essential function for industrial robots. Robotic arms are able to imitate the function of human arms, i.e. linear and spatial translation in two-dimensional or threedimensional space. Robotic arms are commonly
comprised of four parts: the mechanical body, controller, servomotor, and sensor. With the main objective of completing wrist and hand movements, they can correctly repeat countless processes once the operator inputs the action sequences according to operational requirements. Derived from hostile environment, the research and development of mechanical arms is beneficial for laborsaving, reducing the risk of exposure to a hazardous work environment, precision manufacturing, and auxiliary operation. For example, in the harsh environment of an atomic energy laboratory, operating machinery is sometimes necessary to deal with radioactive material, when it is deemed unsafe for human beings. The U.S military also used small robots in hazardous areas to remove bombs in Iraq. Prior to robots being used for bomb removal, bomb-disposal experts had to deactivate bombs, which was potentially life threatening. Currently, bomb-disposal robots stand on the frontline instead of experts, which greatly reduces the risk associated with deactivating bombs. The robotic arm is also used in medicine, such as the da Vinci surgical system [8-9], which is composed of a robotic arm system, surgical platform, and micro image display system. It is the most advanced medical surgical system. Through 3D stereo ultra-high resolution images, the human body tissue structures are shown vividly. The robotic arms used for surgical operation imitate the function of the human hand and wrist joint. Through 360 degrees of dexterity, it can conduct fine surgical operations in a narrow space more precisely than a human hand is capable of. The surgical procedure requires a physician. The doctor typically takes a sitting position while performing an operation and accurately removes focal lesions. The use of a robotic arm aids with long, complex operations.

The emergence of technology has managed to witness the evolvement of a new era known as the Internet of Things (IoT). The Internet of Things (IoT) further describes the internetworking of physical devices, vehicles, buildings, and other items which

[^0]include electronics, software, sensors, actuators, and network connectivity that allow these objects to collect and exchange data. The current revolution of IoT coupled with the growing usage of robots in daily activities have turned the Internet of Robotics Things (IoRT) applications into a tangible reality in the nearest future. The advantage of IoRT is that it allows robotic systems to connect, share, and pass the distributed computation resources, business activities, context information, and environmental data with each other.

The objective of this paper is to combine a touch panel with a robotic arm, thereby constructing a complete human-machine interface control system. There are three motivations: (1) To deeply understand how to analyze the motion model of a robotic arm using the DH algorithm [10-11], and to deduct a theoretical formula of forward kinematics and inverse kinematics, thereby establishing the relationship between the movement angle of various joints of an RRR robotic arm and the 3D position coordinates of the end effector of robotic arm, in order to increase the feasibility of robotic arms. (2) To add to the function of embedded micro controller, thereby increasing the likelihood of feasibility of the mechanical arm. This paper adopted the embedded micro controller AT90CAN128 as the control core chip. It has six sets of PWM output signals, which can directly drive six joint servomotors, and a group of UART serial communications to communicate with the touch panel. Given the perfect integration of the micro control chip and touch panel, the human-machine interface control of the end effector of the robotic arm can be achieved. (3) To embed a wireless transmission module and improve the remote-control ability. As mentioned above, the development of robotic arms was originally motivated to aide with harsh environmental requirements.

## 2 Movement Model of Robotic Arms

The six-axis robotic arm was designed based on the structure of the human arm, as shown in Figure 1. It comprised of six components: a base joint, shoulder joint, elbow joint, bending wrist joint, rotary wrist joint, and finger joint. Each joint is driven by a servo motor. The position and direction of the end of the robotic arm is calculated using robot kinematics. Since the robotic arm is a set of linkages connected with joints, the degree of freedom is the total degree of freedom (DOF) of all the links before connection and fixation, subtracted by the constraint degree of all the joints and the degree of freedom of the fixed links. The number of the DOF is directly related to the motion of the robotic arms. For example, with one DOF, the arm can only move in one direction.


Figure 1. Structure of the human arm and the six-axis robotic arm

The objective of this paper is to determine the position of the end effector in 3D Euclidean space, otherwise known as the coordinates of the wrist joint. Since the posture of rotation is not in the scope of this paper, the rotating wrist joint and finger joints for clipping will not be given consideration. Thus, the sixaxis robotic arm has four DOFs from the base joint, shoulder joint, elbow joint, and bending wrist joint. Denavit and Hartenberg (simplified as D-H) proposed a general method in 1954 to express the geometric relationship of bars in space for robotic kinematics, which is widely employed. In this paper, the D-H coordinate system was adopted. Proper D-H four-link parameters were then defined according to planar RRR six-axis robotic arms, thereby transforming a complicated coupling relationship to a simple transform relationship of a homogeneous matrix.

### 2.1 Transmitting Board for the Wearable Device

### 2.1.1 Establishment of the Coordinate System

As shown in Figure 2, joint $i$ connects rods $i-1$ and $i$. A rigid body coordinate system must be established on each joint. The $i$ th coordinate system must be determined based on the posture of the previous coordinate system, $i-1$. The coordinate systems were established following the rules below:
(1) The axis of joint $i$ is defined as the $z_{i}$ axis of the coordinate system.
(2) The common perpendicular line between $z_{i}$ and $z_{i-1}$ is defined as the $x_{i}$ axis of coordinate system.
(3) The crossover point between the $x_{i}$ axis and $z_{i}$ axis is defined as the origin of the ith coordinate system.
(4) The $y_{i}$ axis is then defined based on the righthand rule.


Figure 2. Definition of the D-H coordinate system and the four-link parameters

Figure 2 Definition of the $\mathrm{D}-\mathrm{H}$ coordinate system and the four-link parameters

### 2.1.2 Parameter Setting of the D-H method

Comparing the $\{i\}_{\text {th }}$ coordinate system and the $\{i+1\}_{\mathrm{th}}$ coordinate system, the rotation angle of each joint and the distance between each connecting rod constitute the four-link parameters of the $\mathrm{D}-\mathrm{H}$ method, namely, $d_{i}, a_{i}, \alpha_{i}$ and $\theta_{i}$. Specifically, $d_{i}$ also called as rod spacing, is the distance between $O_{i}$ and $O_{i+1}$ in the $z_{i}$ direction. $a_{i}$, also called the rod length, is the distance between $O_{i}$ and $O_{i+1}$ in the $x_{i}$ direction. $\alpha_{i}$ is the angle of rotation by moving $z_{i}$ to $z_{i+1}$ along $x_{i} . \theta_{i}$, also called as joint rotation, is the angle of rotation by moving $x_{i}$ to $x_{i+1}$ along $z_{i}$. For a rotating joint, $\theta_{i}$ is a variable. For a translational or sliding joint, $d_{i}$ is a variable.
(1) The joint rotation, $\theta_{i}$ is angle of rotation by moving $x_{i}$ to $x_{i+1}$ along $z_{i}$. The homogeneous transformation matrix between the two coordinate systems is expressed as:

$$
R(z, \theta)=\left[\begin{array}{cccc}
c \theta_{i} & -s \theta_{i} & 0 & 0  \tag{1}\\
s \theta_{i} & c \theta_{i} & 0 & 0 \\
0 & 0 & 1 & 0 \\
0 & 0 & 0 & 1
\end{array}\right]
$$

For convenience, $\cos \left(\theta_{i}\right)$ is simplified as $c \theta_{i}$ and $\sin \left(\theta_{i}\right)$ is simplified as $s \theta_{i}$.
(2) The rod spacing, $d_{i}$ is the distance between $O_{i}$ and $O_{i+1}$ in $z_{i}$ direction. The homogeneous transformation matrix between the two coordinate systems is expressed as:

$$
T(z, d)=\left[\begin{array}{cccc}
1 & 0 & 0 & 0  \tag{2}\\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & d_{i} \\
0 & 0 & 0 & 1
\end{array}\right]
$$

(3) The rod length $a_{i}$ is the distance between $O_{i}$ and $O_{i+1}$ in $x_{i}$ direction. The homogeneous transformation matrix between the two coordinate systems is expressed as:

$$
T(x, a)=\left[\begin{array}{cccc}
1 & 0 & 0 & a_{i}  \tag{3}\\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & 0 \\
0 & 0 & 0 & 1
\end{array}\right]
$$

(4) $\alpha_{i}$ is the angle of rotation by moving $z_{i}$ to $z_{i+1}$ along $x_{i}$. The homogeneous transformation matrix between the two coordinate systems is expressed as:

$$
R(x, \alpha)=\left[\begin{array}{cccc}
1 & 0 & 0 & 0  \tag{4}\\
0 & c \alpha_{i} & -s \alpha_{i} & 0 \\
0 & s \alpha_{i} & c \alpha_{i} & 0 \\
0 & 0 & 0 & 1
\end{array}\right]
$$

Based on the above four transformation matrices, the D-H coordinate transformation matrix from the $\{i\}_{\mathrm{th}}$ coordinate system and the $\{i+1\}_{\text {th }}$ coordinate system can be expresses as:

$$
\begin{align*}
& { }_{i}^{i+1} A=R(z, \theta) T(z, d) T(x, a) R(x, \alpha)  \tag{5}\\
& =\left[\begin{array}{cccc}
c \theta_{i} & -s \theta_{i} c \alpha_{i} & s \theta_{i} s \alpha_{i} & a_{i} c \theta_{i} \\
s \theta_{i} & c \theta_{i} c \alpha_{i} & -c \theta_{i} s \alpha_{i} & a_{i} s \theta_{i} \\
0 & s \alpha_{i} & c \alpha_{i} & d_{i} \\
0 & 0 & 0 & 1
\end{array}\right] \tag{6}
\end{align*}
$$

The $\mathrm{D}-\mathrm{H}$ homogeneous matrix from the $\{0\}$ coordinate system to the $\{i+1\}$ coordinate system can be expressed as:

$$
\begin{equation*}
{ }_{0}^{i} A={ }_{0}^{1} A{ }_{1}^{2} A{ }_{2}^{3} A \cdots{ }_{i-1}^{i} A=\prod_{j=1}^{i}{ }_{j-1}^{j} A \tag{7}
\end{equation*}
$$

### 2.2 Forward Kinematics

In forward kinematics, the position coordinate of the end effector is calculated based on the known axis movement angle of each joint in three-dimensional space. Figure 3 shows the structure and appearance of the six-axis robotic arm. The coordinate systems and related parameters are shown on the left side. In order to simplify the design of this system, it is assumed that the base is fixed without arbitrary rotation, so the rigid axis on the base is always in the same direction. In other words, the robotic arm will only move in one plane, which is referred to as a planar $R R R$ robotic arm. In addition, posture control is not in the scope of this paper, so the finger joint and the rotating wrist joint is not discussed. Figure 4 is the dimensional diagram of the six-axis robotic arm used in this study with an arm
length of 390 mm , a maximum weight of 200 g , and a base disc diameter of 210 mm .


Figure 3. Base-fixed planar RRR four-axis robotic arm


Figure 4. Dimensions of the six-axis robotic arm
The motion equation of the six-axis robotic arm is deduced based on the D-H method. Only the shoulder joint, elbow joint, and bending wrist joint were considered in this study. First, the D-H four-link parameters of each joint were established. The four DH linkage parameters are shown in Table 1.

Table 1. D-H four-link parameters

| Joint (i) | $\alpha_{i}$ <br> Twist Angle | $a_{i}$ <br> Rod Length | $\theta_{i}$ <br> Joint Angle | $d_{i}$ <br> displacement |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | $l_{1}$ | $\theta_{1}$ | 0 |
| 2 | 0 | $l_{2}$ | $\theta_{2}$ | 0 |
| 3 | 0 | $l_{3}$ | $\theta_{3}$ | 0 |

By substituting the parameters from Figure 1 into (6), it follows that:

$$
\begin{align*}
& { }_{0}^{1} A=\left[\begin{array}{cccc}
c \theta_{1} & -s \theta_{1} & 0 & l_{1} c \theta_{1} \\
s \theta_{1} & c \theta_{1} & 0 & l_{1} s \theta_{1} \\
0 & 0 & 1 & 0 \\
0 & 0 & 0 & 1
\end{array}\right]{ }_{1}^{2}, A=\left[\begin{array}{cccc}
c \theta_{2} & -s \theta_{2} & 0 & l_{2} c \theta_{2} \\
s \theta_{2} & c \theta_{2} & 0 & l_{2} s \theta_{2} \\
0 & 0 & 1 & 0 \\
0 & 0 & 0 & 1
\end{array}\right], \\
& { }_{2}^{3} A=\left[\begin{array}{cccc}
c \theta_{3} & -s \theta_{3} & 0 & l_{3} c \theta_{3} \\
s \theta_{3} & c \theta_{3} & 0 & l_{3} s \theta_{3} \\
0 & 0 & 1 & 0 \\
0 & 0 & 0 & 1
\end{array}\right], \tag{8}
\end{align*}
$$

Based on (7), the transformation coordinates from $\{0\}$ to $\{2\}$ and $\{3\}$ are:

$$
\begin{align*}
& { }_{0}^{2} A={ }_{0}^{1} A \cdot{ }_{1}^{2} A=\left[\begin{array}{cccc}
\mathrm{c} \theta_{1} \mathrm{c} \theta_{2}-\mathrm{s} \theta_{1} \mathrm{~s} \theta_{2} & -\mathrm{c} \theta_{1} \mathrm{~s} \theta_{2}-\mathrm{s} \theta_{1} \mathrm{c} \theta_{2} & 0 & l_{1} \mathrm{c} \theta_{1}+l_{2} \mathrm{c} \theta_{12} \\
\mathrm{~s} \theta_{1} \mathrm{c} \theta_{2}+\mathrm{c} \theta_{1} \mathrm{~s} \theta_{2} & -\mathrm{s} \theta_{1} \mathrm{~s} \theta_{2}+\mathrm{c} \theta_{1} \mathrm{c} \theta_{2} & 0 & l_{1} \mathrm{~s} \theta_{1}+l_{2} \mathrm{~s} \theta_{12} \\
0 & 0 & 1 & 0 \\
0 & 0 & 0 & 1
\end{array}\right]  \tag{9}\\
& { }_{0}^{3} A={ }_{0}^{2} A \cdot{ }_{2}^{3} A=\left[\begin{array}{cccc}
c \theta_{123} & -s \theta_{123} & 0 & l_{1} c \theta_{1}+l_{2} c \theta_{12}+l_{3} c \theta_{123} \\
s \theta_{123} & c \theta_{123} & 0 & l_{1} s \theta_{1}+l_{2} s \theta_{12}+l_{3} s \theta_{123} \\
0 & 0 & 1 & 0 \\
0 & 0 & 0 & 1
\end{array}\right](1 \tag{10}
\end{align*}
$$

Herein,

$$
c \theta_{12}=\cos \left(\theta_{1}+\theta_{2}\right), c \theta_{123}=\cos \left(\theta_{1}+\theta_{2}+\theta_{3}\right) .
$$

Forward kinematics is used to derive the homogeneous matrix of the whole structure, including the posture and position vectors of the arm, as shown in (11). The $3 / 3 r$ elements in the top left matrix is the rotation matrix, or posture matrix, and $Q_{x}, Q_{y}$ and $Q_{z}$, on the right are the position vectors. The position and posture after movement is obtained by applying the homogeneous matrix.

$$
\begin{align*}
& { }_{0}^{i} A={ }_{0}^{1} A{ }_{1}^{2} A{ }_{2}^{3} A \cdots{ }_{i-1}^{i} A \\
& =\prod_{j=1}^{i}{ }_{j-1}^{j} A=\left[\begin{array}{cccc}
r_{11} & r_{12} & r_{13} & Q_{x} \\
r_{21} & r_{22} & r_{23} & Q_{y} \\
r_{31} & r_{32} & r_{33} & Q_{z} \\
0 & 0 & 0 & 1
\end{array}\right] \tag{11}
\end{align*}
$$

According to the above discussion, the coordinates of the center point of the rotating wrist joint can be calculated by (10).

$$
\begin{gather*}
Q_{x}=l_{1} \cos \theta_{1}+l_{2} \cos \left(\theta_{1}+\theta_{2}\right)+l_{3} \cos \left(\theta_{1}+\theta_{2}+\theta_{3}\right)  \tag{12}\\
Q_{y}=l_{1} \sin \theta_{1}+l_{2} \sin \left(\theta_{1}+\theta_{2}\right)+l_{3} \sin \left(\theta_{1}+\theta_{2}+\theta_{3}\right) \tag{13}
\end{gather*}
$$

The coordinates of the center point of the bending wrist joint can be calculated by (9).

$$
\begin{align*}
& P_{x}=l_{1} \cos \theta_{1}+l_{2} \cos \left(\theta_{1}+\theta_{2}\right)  \tag{14}\\
& P_{y}=l_{1} \sin \theta_{1}+l_{2} \sin \left(\theta_{1}+\theta_{2}\right) \tag{15}
\end{align*}
$$

### 2.3 Inverse Kinematics

According to inverse kinematics, the rotation angle of each joint is calculated based on known spatial coordinates, Q , of the end effector of the robotic arm. Figure 5 shows a base-fixed planar RRR four-axis robotic arm on the left side.


Figure 5. Inverse kinematics
Assuming that the coordinates of the center point of the rotating wrist joint are ( $Q_{x}, Q_{y}$ ), the coordinates of the center point of the bending wrist joint are $\left(P_{x}, P_{y}\right)$, and the orientation angle of the end of the robotic arm is $\phi$, the joint angles $\theta_{1}, \theta_{2}, \theta_{3}$ were calculated. The orientation angle of the end of the robotic arm is defined as:

$$
\begin{equation*}
\theta_{123}=\theta_{1}+\theta_{2}+\theta_{3}=\phi \tag{16}
\end{equation*}
$$

The relationship between the coordinates of the rotating joint, Q , and the coordinates of the bending wrist joint, P , can be expressed as:

$$
\begin{align*}
& P_{x}=Q_{x}-l_{3} \cos (\phi)=l_{1} \cos \theta_{1}+l_{2} \cos \left(\theta_{1}+\theta_{2}\right)  \tag{17}\\
& P_{y}=Q_{y}-l_{3} \sin (\phi)=l_{1} \sin \theta_{1}+l_{2} \sin \left(\theta_{1}+\theta_{2}\right) \tag{18}
\end{align*}
$$

For convenience, the four-axis robotic arm is simplified into a three-axis robotic arm. Based on the coordinates of the bending wrist joint ( $P_{x}, P_{y}$ ), the rotation angle of each joint is calculated using inverse kinematics. From Figure 5, it can be observed that:

$$
\begin{equation*}
\beta^{2}=P_{x}^{2}+P_{y}^{2}, \lambda=l_{2} \sin \theta_{2}, \gamma=l_{2} \cos \theta_{2} \tag{19}
\end{equation*}
$$

It can be further simplified to:

$$
\begin{align*}
& \beta^{2}=\lambda^{2}+\left(l_{1}+\gamma\right)^{2}=\left(l_{2} \sin \theta_{2}\right)^{2}+\left[l_{1}+\left(l_{2} \cos \theta_{2}\right)\right]^{2}  \tag{20}\\
& =l_{1}^{2}+l_{2}^{2}+2 l_{1} l_{2} \cos \theta_{2}
\end{align*}
$$

Therefore, the rotation angle, $\theta_{2}$ of the elbow joint is obtained from (19) and (20).

$$
\begin{equation*}
\theta_{2}=\cos ^{-1}\left(\frac{P_{x}^{2}+P_{y}^{2}-l_{1}^{2}-l_{2}^{2}}{2 l_{1} l_{2}}\right) \tag{21}
\end{equation*}
$$

From (11), although both $P_{x}$ and $P_{y}$ contain positive and negative values, the rod length $l_{1}$ and $l_{2}$ remain positive. In the area range of $\theta_{2}$ which the robotic arm can reach, $\theta_{2}$ calculated by (11) will be positive. The negative sign of $\theta_{2}$ can only be determined based on the values of $P_{x}$ and $P_{y}$. The following situations will be discussed:
(1) When $\left|P_{x}^{2}+P_{y}^{2}-l_{1}^{2}-l_{2}^{2}\right|<1 \quad 0<\theta_{2}<90^{\circ}$ or $-90^{\circ}<$ $\theta_{2}<0^{0}$
(2) When $\left|P_{x}^{2}+P_{y}^{2}-l_{1}^{2}-l_{2}^{2}\right|=1$, the robotic arm is either in the state of extension or in a folded condition.
(3) When $\left|P_{x}^{2}+P_{y}^{2}-l_{1}^{2}-l_{2}^{2}\right|>1$, the robotic arm is not able to reach the position.

The angle range of the servo motors used in the system is $0<\theta_{2}<60^{\circ}$ or $-60^{\circ}<\theta_{2}<0^{\circ}$. In other words, only when the following conditions $0.5<P_{x}^{2}+P_{y}^{2}-l_{1}^{2}-l_{2}^{2}<1$ and $-1<P_{x}^{2}+P_{y}^{2}-l_{1}^{2}-l_{2}^{2}<-0.5$ are satisfied, can the robotic arm reach the position.

Then, the rotation angle, $\theta_{1}$ of the elbow joint is deducted according to (14) and (15).

$$
\begin{align*}
& P_{x}=l_{1} \cos \left(\theta_{1}\right)+l_{2} \cos \left(\theta_{1}+\theta_{2}\right)  \tag{22}\\
& P_{y}=l_{1} \sin \left(\theta_{1}\right)+l_{2} \sin \left(\theta_{1}+\theta_{2}\right) \tag{23}
\end{align*}
$$

Based on the product to sum formula, (14) and (15) can be simplified as:

$$
\begin{gather*}
P_{x}=l_{1} \cos \theta_{1}+l_{2} \cos \theta_{1} \cos \theta_{2}-l_{2} \sin \theta_{1} \sin \theta_{2}  \tag{24}\\
P_{y}=l_{1} \sin \theta_{1}+l_{2} \sin \theta_{1} \cos \theta_{2}+l_{2} \cos \theta_{1} \sin \theta_{2} \tag{25}
\end{gather*}
$$

It can be further simplified as:

$$
\begin{gather*}
P_{x}=\left(l_{1}+l_{2} \cos \theta_{2}\right) \cos \theta_{1}-\left(l_{2} \sin \theta_{2}\right) \sin \theta_{1}  \tag{26}\\
P_{y}=\left(l_{2} \sin \theta_{2}\right) \cos \theta_{1}+\left(l_{1}+l_{2} \cos \theta_{2}\right) \sin \theta_{1} \tag{27}
\end{gather*}
$$

Assuming $\cos \theta_{1}$ and $\sin \theta_{1}$ are two unknown variables, and (26) and (15) are dual linear equations, then

$$
\begin{align*}
& \sin \theta_{1}=\frac{\left(l_{1}+l_{2} \cos \theta_{2}\right) P_{y}-\left(l_{2} \sin \theta_{2}\right) P_{x}}{\left(l_{1}+l_{2} \cos \theta_{2}\right)^{2}+\left(l_{2} \sin \theta_{2}\right)^{2}}  \tag{28}\\
& \cos \theta_{1}=\frac{\left(l_{1}+l_{2} \cos \theta_{2}\right) P_{x}+\left(l_{2} \sin \theta_{2}\right) P_{y}}{\left(l_{1}+l_{2} \cos \theta_{2}\right)^{2}+\left(l_{2} \sin \theta_{2}\right)^{2}} \tag{29}
\end{align*}
$$

the rotation angle of the elbow joint is:

$$
\begin{equation*}
\theta_{1}=\tan ^{-1}\left(\frac{\left(l_{1}+l_{2} \cos \theta_{2}\right) P_{y}-\left(l_{2} \sin \theta_{2}\right) P_{x}}{\left(l_{1}+l_{2} \cos \theta_{2}\right) P_{x}+\left(l_{2} \sin \theta_{2}\right) P_{y}}\right) \tag{30}
\end{equation*}
$$

Once $\theta_{1}$ and $\theta_{2}$ are obtained by (21) and (30), the rotation angle of the bending wrist joint is:

$$
\begin{equation*}
\theta_{3}=\phi-\theta_{1}-\theta_{2} \tag{31}
\end{equation*}
$$

Herein, $\phi=\tan ^{-1} Q_{y} / Q_{x}$.

## 3 System Architecture of the Six-axis Robotic Arm

The primary objective for this system is to use an embedded microprocessor and touch panel as the main control platform, along with an ATMEL microcontroller as the core chip, in order to completely control the sixaxis robotic arm. As this solution is different from traditional personal computer control platforms, it can greatly reduce the system cost and has the advantage of portability. Figure 6 shows the structure of the system. The system consists of a six-axis robotic arm, a WEINTEK touch panel, and an AT90CAN128 core chip PWM control panel.


Figure 6. System architecture of the six-axis robotic arm
Figure 7 shows the structure of the robotic arm used in this study. The mechanical specifications are: (1) net weight: 2 kg , (2) arm length: 390 mm , (3) maximum distance of claw: 53 mm , (4) two Micro STD servo motors with 1.8 kg torque, (5) four metal gear servo motors with 12 kg torque, (6) 6 DOFs , (7) maximum lifting force: 200 g (at $6 \mathrm{~V} / 3$ A working voltage), (8) aluminum alloy structure with super metal texture, which is scratch proof on the surface of aluminum parts. The electrical specifications are: (1) working voltage 4.8-6 V, (2) power consumption of servo motors: 2-3 A, (3) control core chip AT90CAN128. The mechanical arm is composed of six servo motors (including a reduction gearbox reducer and a PID control circuit), which correspondingly control the rotation of the base joint, lift of the shoulder joint, swing of the elbow joint, rotation and bending of the wrist joint, and clamping of the finger joint. The base, shoulder, elbow, and rotating wrist joints are driven by 12 kg torque metal gear servo motors, while the bending wrist and finger joints are driven by 1.8 kg
torque servo motors. The characteristics of the metal gear servo motor are as follows: (1) dimensions: 40.4 x $9.8 \times 36 \mathrm{~mm}$, (2) weight: 48 g , (3) speed: $0.22 \mathrm{sec} / 60^{\circ}$, (4) output torque: $12 \mathrm{~kg}-\mathrm{cm}$. In addition, the characteristics of the DGServoS05NF STD servo motors are: (1) dimensions: $28 / 14 / 59.8 \mathrm{~mm}$, (2) weight: 18 g , (3) speed: $0.13 \mathrm{sec} / 60^{\circ}$, (4) output torque: $1.8 \mathrm{~kg}-\mathrm{cm}$. Rubber pads were assembled in the inner side of the fixture in order to increase the grasping friction. Figure 7 shows the specifications of the sixaxis robotic arm. Figure 8 shows the fixture of finger joint.


Figure 7. Specifications of the six-axis robotic arm


Figure 8. Fixture of finger joint

## 4 Tests and Results

### 4.1 Tests of Six-axis Joint Motors

Figure 9 shows the position of the six-axis robotic arm when the base joint, shoulder joint, elbow joint, bending wrist joint, rotating wrist joint, and finger joint rotate $-60^{\circ},-60^{\circ}, 50^{\circ},-20^{\circ}, 0^{\circ}$, and $30^{\circ}$, respectively. Figure 10 shows the position of the arm when the base joint, shoulder joint, elbow joint, bending wrist joint, rotating wrist joint, and finger joint rotate $30^{\circ},-60^{\circ}$, $50^{\circ},-20^{\circ}, 0^{\circ}$, and $30^{\circ}$, respectively. The difference
between the two conditions is that the base joint moves to the left by $60^{\circ}$ in the first condition, while it moves to the right by $30^{\circ}$ in the second. Figure 11 shows the position of the arm when the base joint, shoulder joint, elbow joint, bending wrist joint, rotating wrist joint, and finger joint rotate $30^{\circ}, 30^{\circ}, 50^{\circ},-20^{\circ}, 0^{\circ}$, and $30^{\circ}$, respectively.


Figure 9. Test (I) of the six-axis joint motors


Figure 10. Test (II) of the six-axis joint motors


Figure 11. Test (III) of the six-axis joint motors

### 4.2 Integration Test

In this section, an integration test is described.

Specifically, two tests were conducted. In the first test, the aim was to move the end effector (rotating wrist joint) and bending wrist joint to the following coordinate position:
( $P_{x}=120 \mathrm{~mm}, P_{y}=105 \mathrm{~mm}, Q_{x}=135 \mathrm{~mm}, Q_{y}=150 \mathrm{~mm}$ )
In the second test, the aim was to move the end effector (rotating wrist joint) and bending wrist joint to the following coordinate position:
$\left(P_{x}=-138 \mathrm{~mm}, P_{y}=158.9 \mathrm{~mm}, Q_{x}=-175 \mathrm{~mm}, Q_{y}=\right.$ 95 mm )

On the human-machine interface of the WEINTEK touch panel MT6071iE, when the button "inverse kinematics" is pressed, a window (as shown in Figure 12) will pop up. In the window, the coordinates of the bending wrist joint $\left(P_{x}, P_{y}\right)$ and the rotating wrist joint $\left(Q_{x}, Q_{y}\right)$ can be entered. Pressing the button "Calculation of inverse kinematics" displays that the angle of the shoulder joint motor $\theta 1=33^{\circ}$, the angle of the elbow joint motor $\theta 2=16^{\circ}$, and angle of the bending wrist joint motor $\theta 3=22$, as shown in Figure 12.


Figure 12. Results of the first test from inverse kinematics

Similarly, in the second test, it is obtained that the angle of shoulder joint $\theta 1=-43^{\circ}$, the elbow joint $\theta 2=$ $34^{\circ}$, and bending wrist joint $\theta 3=-30^{\circ}$, as shown in Figure 13.


Figure 13. Results of the second test from inverse kinematics

In the second step, by pressing the button "download parameters", the WEINTEK MT6071iE sends the movement angle data of every joint to the motor drive board AT90CAN128 via an RS232 serial communication port. The micro controller then generates a PWM pulse modulation signal to drive the six-axis robotic arm towards the target position. Once


Figure 14. Coordinate measurement of Point $P$ in the first test
the robotic arm reaches the position, the coordinates of points Q and P are measured with a ruler.

The measured coordinates of the first test are: (as shown in Figure 14, Figure 15 and Table 2).

$$
\begin{aligned}
& P\left(P_{x}=119.5 \mathrm{~mm}, P_{y}=108 \mathrm{~mm}\right) \\
& Q\left(Q_{x}=134.5 \mathrm{~mm}, Q_{y}=149.5 \mathrm{~mm}\right)
\end{aligned}
$$



Figure 15. Coordinate measurement of Point $Q$ in the first test

Table 2. Comparison of the theoretical and measurement values of the coordinates of P and Q in the first test

| Theoretic value |  |  | Ideal value/Actual vale/Error value |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Shoulder | Elbow | Bending wrist |  |  | Wrist | nt (P) |  |  |  |  | Wrist | int (Q) |  |  |
| $\begin{gathered} \theta 1 \\ (\mathrm{deg}) \end{gathered}$ | $\begin{gathered} \theta 2 \\ (\mathrm{deg}) \end{gathered}$ | $\begin{gathered} \theta 3 \\ (\mathrm{deg}) \end{gathered}$ | $\begin{gathered} \mathrm{Px} \\ \text { Ideal } \\ \text { value } \end{gathered}$ |  | $\begin{gathered} \text { Px } \\ \text { Error } \end{gathered}$ | $\begin{gathered} \text { Py } \\ \text { Ideal } \\ \text { value } \end{gathered}$ |  | $\begin{gathered} \text { Py } \\ \text { Error } \end{gathered}$ | $\begin{gathered} \mathrm{Qx} \\ \text { Ideal } \\ \text { value } \end{gathered}$ | Qx <br> Actual <br> value | $\begin{gathered} \mathrm{Qx} \\ \text { Error } \end{gathered}$ | $\begin{gathered} \text { Qy } \\ \text { Ideal } \\ \text { value } \end{gathered}$ | Qy Actual value | $\begin{gathered} \text { Qy } \\ \text { Error } \end{gathered}$ |
| 33 | 16 | 22 | 120.0 | 119.5 | 0.5 | 105.0 | 108.0 | -3 | 135.0 | 134.5 | 0.5 | 150.0 | 149.5 | 0.5 |

The measured coordinates of the second test are: (as shown in Figure 16, Figure 17 and Table 3).

$$
\begin{gathered}
P\left(P_{x}=-138 \mathrm{~mm}, P_{y}=68 \mathrm{~mm}\right) \\
Q\left(Q_{x}=-175 \mathrm{~mm}, Q_{y}=98 \mathrm{~mm}\right)
\end{gathered}
$$

## 5 Conclusions

In the current study, the robotic arm is comprised of six joints, which are powered by six servomotors (including reduction gear and a PID control circuit). The servomotors perform the rotation of the base joint, lifting of the shoulder joint, swing of the elbow joint, rotation and bending of the wrist joint, and grasping of the finger joint. The primary objective of this system is to use an embedded microprocessor and a touch panel
as the main control platform, along with an ATMEL microcontroller as the core chip, in order to have full control of the six-axis robotic arm. As this system is different from the traditional personal computer control platform, it can greatly reduce the system cost, and has the advantage of portability. Currently, using the third generation AT90CAN128 chip as the micro controller meets the current working requirement. However, it might be unable to cope with the calculation work if given more functions. In future work, the AT90CAN128 microcontroller should be replaced with a fourth-generation ARM embedded microprocessor, in order to cope with a heavier computational load. Also, Touch Panel will be developed into an IoT system (including web pages and cloud servers). The Touch Panel can be removed via a mobile phone, laptop or computer to control a six-axis robotic arm.


Figure 16. Coordinate measurement of Point $P$ in the second test


Figure 17. Coordinate measurement of point $Q$ in the second test

Table 3. Comparison of the theoretical and measurement values of the coordinates of $P$ and $Q$ in the second test

| Theoretic value |  |  | Ideal value/Actual vale/Error value |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Shoulder | Elbow | Bending wrist | Wrist joint (P) |  |  |  |  |  | Wrist joint (Q) |  |  |  |  |  |
| $\begin{gathered} \theta 1 \\ (\mathrm{deg}) \end{gathered}$ | $\begin{gathered} \theta 2 \\ (\mathrm{deg}) \end{gathered}$ | $\begin{gathered} \theta 3 \\ (\mathrm{deg}) \end{gathered}$ |  |  | $\begin{gathered} \mathrm{Px} \\ \text { Error } \end{gathered}$ | $\begin{gathered} \text { Py } \\ \text { Ideal } \\ \text { value } \end{gathered}$ |  | $\begin{gathered} \text { Py } \\ \text { Error } \end{gathered}$ | $\begin{gathered} \mathrm{Qx} \\ \text { Ideal } \\ \text { value } \end{gathered}$ | Qx Actual value | $\begin{gathered} \text { Qx } \\ \text { Error } \end{gathered}$ | $\begin{gathered} \mathrm{Qy} \\ \text { Ideal } \\ \text { value } \end{gathered}$ | Qy Actual value | $\begin{gathered} \text { Qy } \\ \text { Error } \end{gathered}$ |
| -44 | 35 | -29 | -137.5 | -138.0 | 0.5 | 68.0 | 68.0 | 0.0 | 175.0 | 175.0 | 0.0 | 97.8 | 95.0 | 2.8 |

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