

# An ECC Based Remote User Authentication Protocol

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## Abstract

IoT has remarkably broaden the universal network of information barter, because millions of the communication devices have become the ingredients of global network. Apart from the abundant advantages of the expansion of global network, secure authentication and communication between global networking elements are posing numerous challenges. To expedite user authenticity with the help of elliptic curve cryptography a new efficient scheme is introduced in contrast to the previous schemes. Security analysis of proposed scheme is affirmed through random oracle model. Moreover, performance and security analysis show that the proposed scheme prevents the major attack and provides additional security features. The performance analysis is carried out by implementing the proposed protocol using python language in ubuntu. Thus, because of the better security and performance, proposed protocol is adequate for the resource constrained and security sensitive environments.

**Keywords:** Remote-User, ECC, Authentication, Ubuntu, Pycharm

## 1 Introduction

Rapid growth of wireless communication technologies has laid a very powerful impact on our life. A very large community in the world are getting the benefits of the wireless technology via wireless devices like mobile phones, notebooks and various other wireless devices. Due to these wireless devices, large amount of people at any location and at any time are enjoying the online services. There are various kinds of online services being provided, such as web browsing, video calls, telemedicine system and government assistance. An attacker can easily eavesdrop the information shared between legal users and can also change or intercept information. It is due to the fact that the Internet structure is still prone to attacks, as it is easily accessible to anyone. To make the shared messages secure between legal participants,

we need an authentication protocol. Early on authentication protocol were based on single factor i.e. password. As the first attempt only, Lamport [1] introduced password based authentication protocol. Therefore, many people started working on password based authentication protocols and many password based protocols were developed by researchers [2-7].

Although, password based authentication attracted the researchers and provided a foundation for new protocols. Later on, it is realized that just password based authentication is not enough as it can easily be cracked. After that, researchers proposed two-factor authentication protocols [8-17] to bring more security. In two factor authentication protocols, smart card of the user is used as the additional factor along with password.

Though, two-factor authentication protocols provide more reliability and security but many systems are constrained in terms of resource utilization in communication technologies. However, these systems obliged two-factor authentication protocols that include lightweight computational operations like hash operations and arbitrary numbers. To accomplish reasonable security, a computationally effective and efficient protocol is proposed by Tsai et al. [18], which uses hash operations and arbitrary numbers. Many other lightweight protocols are also developed in [19-21], in which security has been compromised to a certain level by minimizing the computation cost. We determine that lightweight protocols does not provide enough security and reliability and thus these protocols are prone to attacks easily [22-23].

To decrease the cost of transmission and computation, Juang et al. [24] used the ECC based system for the session key exchange and authentication protocol. Xu et al. [25] observed that two protocols of Lee et al. [26-27] are not secure against password guessing and impersonation attacks, they proposed a more efficient two-factor based protocol against the described attacks. Further, Juang et al. demonstrates the enhanced security feature of their protocol by using the Diffie-Hellman protocol's assumption.

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Later, Sood et al. [28] and Song [29] discovered that the Xu et al.'s protocol does not give much security against masquerading and privileged insider attacks. Therefore, they proposed an improved protocol that provides security against the expected security threats. After that, Chen et al. [30] performed the analysis of both the enhanced protocols and stated that Sood et al.'s protocol is not offering mutual authentication also Song et al.'s protocol does not resist password guessing and smart card stolen attack. Therefore, Chen et al. proposed a better scheme and claimed that their enhanced scheme provides security against many attacks. Afterwards, Jiang et al. identified that Chen et al.'s protocol does not resist offline dictionary attack, also does not maintain anonymity of the user.

Qu and Tan [31] then proposed two factor based key exchanging protocol for mutual authentication. However, Huang et al. [32] showed that Qu et al.'s scheme is still prone to smart card stolen and masquerading attack. Therefore, Huang et al. proposed an enhanced authentication and key exchanging protocol. Then, Chaudhry et al. [33] claimed that Huang et al.'s protocol does not resist user masquerading attack and also proposed an enhanced scheme that prevent this attack. Moreover, we have analyzed that Chaudhry et al. [32] scheme is still vulnerable to smart card stolen attack. In 2017, Nikooghdam et al. [34] presented a authentication protocol later which was cryptanalyzed by Limbasiya et al. [35] meanwhile many other RUA protocols were presented [36-46].

In this paper, we have presented more secure, efficient and lightweight remote user key exchanging protocol. Architecture for remote-user authentication is shown in Figure. 1.

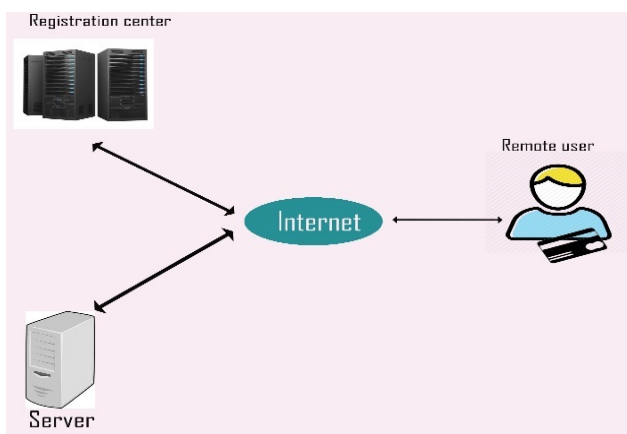


Figure 1. Remote-user authentication

### 1.2 Motivation and our Contribution

The protocols for authentication of user should be lightweight and secure. Several protocols are presented in recent time but those protocols not provides enough security also they are not lightweight. To remove above described flaws we proposed, a new ECC based

remote user authentication scheme. Our presented scheme has several advantages which are as follows:

1. By sharing the session key, the server and user can validate each other.
2. Presented protocol secures identity of user from the attacker/adversary.
3. Attacker/adversary is unable to calculate the session key if he has the smart card of the user.
4. Presented scheme provides security against major attacks.
5. Protocol is efficient in terms of resource utilization.

### 1.3 Paper Structure

This paper is divided into the following sections: Sect.1 presents introduction. In Sect.2 , preliminaries are demonstrated. In Sect.3, our proposed protocol is described. Sect.4, describes the formal security analysis of proposed scheme. In Sect.5, there is performance and security comparison. In Sect.6, presented work is concluded.

## 2 Preliminaries

In this section, the major basics of the commonly used adversarial model, ECC, hash function and several notations used in this paper are described. Some commonly used notations are shown in Table 1.

### 2.1 Proposed Architecture for Remote User Authentication

Figure 2 shows that  $U_r$  through his smart card register himself on the server via a secure channel whereas an attacker has no access of the secure channel. Figure 3 depicts the login and authentication phase  $U_r$  send login request to server via a public channel, however adversary has the access to public channel and can eavesdrop, intercept, and modify the message.



Figure 2. Remote user registration

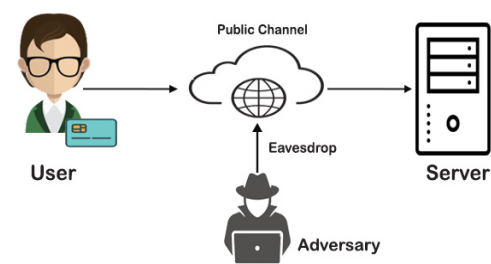


Figure 3. Remote user login and authentication

## 2.2 Elliptic Curve Cryptography (ECC)

The equation of Elliptic curve has defined in the form  $E_p(a,b):x^2 = y^3 + ax + b$  over a prime finite field  $(x, y) \in W_p^* \times W_p, a, b$  and  $4a^3 + 27b^2 \neq 0(\text{mod } P)$  in which  $P$  is a selected huge prime number, the size of  $P$  is  $\geq 160$  bits. Scalar product is gained by repeated addition e.g.,  $nt = t + t + t + \dots + t$  ( $n$  times), over a determined  $t$  a point on  $E_p(e, f)$  and the multiplier  $n$ . The variables  $(e, f, t, P, n)$  should be the member of limited field  $F_p$ . The  $E$  is supposed to be the abelian group, whereas  $O$  is stated as the  $ID$ 's infinity point.

**Table 1.** Notation table

Symbols	Details
$U_r$	$r^{\text{th}}$ Legitimate user
$ID_r$	User identity
$PW_r$	User password
$S$	Legitimate server
$ssk$	Server's private key
$spk$	Server's public key
$SC_r$	User's Smart card
$SK$	Session Key
$a_r$	Random number chosen by $U_r$ during registration phase
$\oplus$	XOR operator
$\parallel$	Concatenation operator
$h$	Hash function

### Definition 1 (Logarithmic issues in ECDLP)

ECDLP: Given two specified points over  $R, V \in E_p(e, f)$ , calculate  $n$  a scalar so that  $R = nV$ . The chances that attacker  $A$  can find  $n$  in the polynomial time ( $T$ ) are described as  $Adv_X^{ECDLP}(T) = pr[(X(R, V) = x : xx \in W_p)]$ . ECDLP assumption concludes that  $Adv_X^{ECDLP}(T) \leq \epsilon$ .

## 2.3 Hash Function

By taking an input string  $O = H(String)$  of random size, a fixed size output is generated by hash. Generated output is called hash code. A little change in the value of string can cause a huge difference. Whereas, a secure hash function has following specifications.

- If the string is described, it's easy to compute  $O = H(String)$ .
- If  $O = H(String)$  is described, it is impossible to find out the string.
- It is tedious task to distinguish input of  $String_1$  and  $String_2$  so that  $H(String_1) = H(String_2)$ . This property is named as collision resistance.

### Definition (Characteristics of Collision Resistance)

Secure hash function  $H(.)$  is predetermined for collision resistance. The possibility that an attacker  $A$  can find a pair  $(String_1 \neq String_2)$  as  $H(String_1) = H(String_2)$  is separated as  $Adv_A^{HASH}(t) = prb[(String_1, String_2) \leftarrow_r A : (String_1 \neq String_2), H(String_1) = H(String_2)]$ , where attacker is allowed to choose a pair  $(String_1, String_2)$  randomly. Attacker's perk is calculated against the random selections taken with-in polynomial time ( $t$ ). Further, Collision resistance conclude that  $Adv_A^{HASH}(t) \leq \epsilon$  whereas  $\epsilon < 0$ , is an enough tiny amount.

## 2.4 Adversarial Model

The basic adversarial model as stated in [44-46] is described in this paper. Following steps were taken up according to the ability of the attacker  $A$ :

- (1)  $A$  has control over all the communication channels which are public.  $A$  can extract, replay, update, abolish or communicate a new replicated message.
- (2)  $A$ , through power analysis, can get or leak out [47-50] the stored information in a smart card.
- (3)  $A$  may be a deceitful or intruder user or the server.
- (4) The identities of servers and users are not private but familiar to insiders.
- (5)  $A$  cannot instigate attack on the server as it is thought to be secure.

## 3 Proposed Scheme

This section discusses the proposed protocols for remote user authentication. Proposed protocol provides desired security to make it invincible against major security attacks and is more efficient than previous remote user authentication schemes.

### 3.1 Registration Phase

For registering the user, each user  $U_r$  chooses his  $ID_r, PW_r$  and  $a_r$ . After that  $U_r$  calculate  $RP_r$  by applying functions of one way hash that is embedded with the concatenation of  $PW_r$  and  $a_r$ . Then  $U_r$  sends,  $\{ID_r, RP_r\}$  to  $S$ , via a protected channel. On receiving these values,  $S$  calculates:

$$\begin{aligned} \alpha_r &= h(ID_r \parallel ssk) \\ \beta_r &= RP_r \oplus \alpha_r \\ \lambda_r &= h(ID_r \parallel RP \parallel \alpha_r) \end{aligned}$$

$S$  via a protected channel, then reserve the  $\beta_r$  and  $\lambda_r$  in  $U_r$ 's smart card. The  $U_r$  then inserts  $a_r$  in

smart card after receiving it from server  $S$ . Now, the smart card contains these values  $\{\beta_r, \lambda_r, a_r\}$ .

### 3.2 Login Phase

Step LO 1:  $U_r$  inserts the smart card in the card reader and enters his unique  $ID_r$  and  $PW_r$ . Smart card  $SC_r$  then calculates:

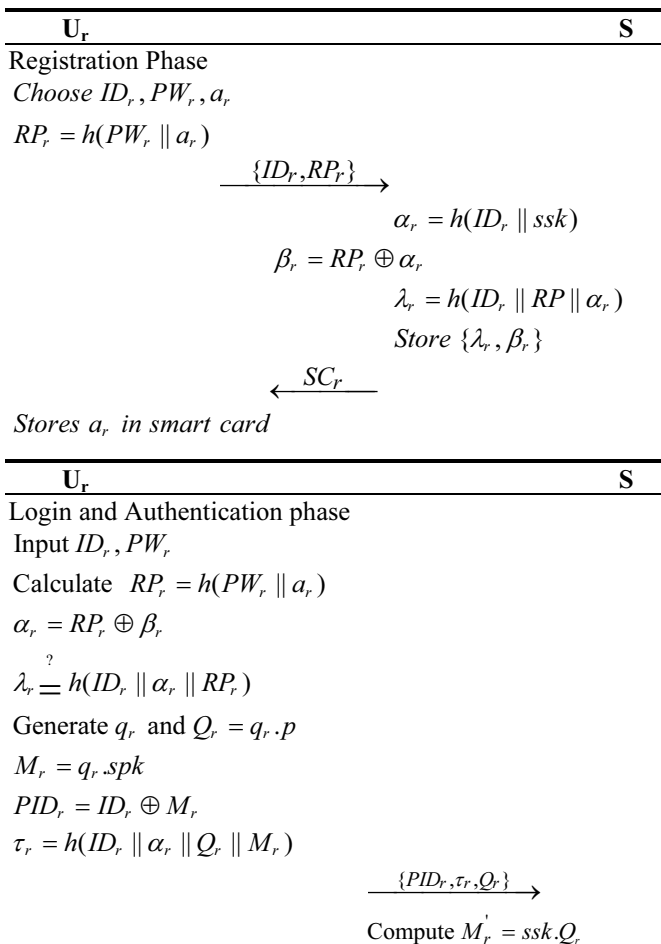
$$\begin{aligned}
 RP_r &= h(PW_r \parallel a_r) \\
 \alpha_r &= RP_r \oplus \beta_r \\
 \lambda_r &= h(ID_r \parallel \alpha_r \parallel RP_r)
 \end{aligned}$$

Then,  $U_r$  checks that the  $\lambda_r$  equals to value stored in smart card. If both of these values are equal then the unique  $ID_r$  and  $PW_r$  is considered valid, else the session will be terminated.

Step LO 2: Smart card capitulates  $q_r$  and calculates  $Q_r = q_r \cdot p$  whereas,  $p$  is a point on elliptic curve. Moreover, computes:

$$\begin{aligned}
 M_r &= q_r \cdot spk \\
 PID_r &= ID_r \oplus M_r \\
 \tau_r &= h(ID_r \parallel \alpha_r \parallel Q_r \parallel M_r)
 \end{aligned}$$

After calculating these values, user  $U_r$  sends  $\{PID_r, \tau_r, Q_r\}$  towards  $S$ .



$$\begin{aligned}
 ID_r' &= PID_r \oplus M_r' \\
 \tau_r' &= h(ID_r' \parallel \alpha_r \parallel Q_r \parallel M_r')
 \end{aligned}$$

Check  $\tau_r' \stackrel{?}{=} \tau_r$   
 Generate  $q_s$   
 Compute  $Q_s = q_s \cdot Q_r$   
 $N_s = Q_s \oplus M_r$   
 $\tau_s = h(\alpha_r \parallel ID_r \parallel Q_s)$

$$\xleftarrow{\{N_s, \tau_s\}}$$

$$\begin{aligned}
 Q_s' &= N_s \oplus M_r \\
 \tau_s' &= h(\alpha_r \parallel ID_r \parallel Q_s) \\
 \tau_s' &= \tau_s
 \end{aligned}$$

$$SK = h(ID_r \parallel Q_r \parallel Q_s \parallel M_r)$$

### Proposed Scheme

### 3.3 Authentication Phase

For authenticating,  $S$  performs following steps against login entries that the user  $U_r$  sends.

Step AU 1: After receiving login request server computes:

$$\begin{aligned}
 M_r' &= ssk \cdot Q_r \\
 ID_r' &= PID_r \oplus M_r' \\
 \tau_r' &= h(ID_r' \parallel \alpha_r \parallel Q_r \parallel M_r')
 \end{aligned}$$

After that  $S$  inspects either  $\tau_r' \stackrel{?}{=} \tau_r$  if the condition does not hold true then session will be aborted, otherwise  $U_r$  is supposed as legitimate user. Then server  $S$  generates arbitrary number  $q_s$  and further computes:

$$\begin{aligned}
 Q_s &= q_s \cdot Q_r \\
 N_s &= Q_s \oplus M_r \\
 \tau_s &= h(\alpha_r \parallel ID_r \parallel Q_s)
 \end{aligned}$$

Server then sends  $\{N_s, \tau_s\}$  against the login request from the user  $U_r$ .

Step AU 2:  $U_r$  then calculates

$$\begin{aligned}
 Q_s' &= N_s \oplus M_r \\
 \tau_s' &= h(\alpha_r \parallel ID_r \parallel Q_s)
 \end{aligned}$$

$U_r$  checks the condition  $\tau_s' = \tau_s$ . Session will abort if this condition does not hold true, else  $U_r$  computes session key as follows:

$$SK = h(ID_r \parallel Q_r \parallel Q_s \parallel M_r)$$

## 4 Security Analysis

### 4.1 Informal Security Analysis

In this portion the proposed protocols of security analysis has explained. The security analysis demonstrates that our proposed scheme prevents all the major possible attacks. Detailed analysis is given below.

#### 4.1.1 Smart Card Stolen Attack

Let's suppose an adversary  $A$  steals the  $U_r$ 's smart card and retrieves values  $\beta_r, \lambda_r$  and an arbitrary number  $a_r$ . Still  $A$  can not extract  $ID_r$  because, to calculate correct value of  $\beta_r$ ,  $A$  needs to server's private key  $ssk$ . To calculate the value of  $\lambda_r$ , he needs  $RP_r$  which includes  $PW_r$  of  $U_r$ . That's why it is not beneficial for  $A$ , even if he steals the smart card of  $U_r$ .

#### 4.1.2 User's Privacy and Anonymity

$U_r$  identity is not transferred in plain text in proposed protocol. Further, the smart card leaves no traces of  $U_r$ 's identity. Moreover, the calculation of  $Q_r = q_r \cdot p$  consists of random number  $q_r$ , whereas the random number is session specific. Therefore, it is hard to extract  $ID_r$  of legal  $U_r$  and to find out that either same  $U_r$  has initiated the two or more different sessions.

#### 4.1.3 Mutual Authentication

In our proposed protocol,  $S$  authenticates  $U_r$  by checking whether  $\tau_r' = \tau_r$ . If an adversary wants to compute  $\tau_r$  correctly, he has to compute  $h(ID_r' \parallel \alpha_r \parallel Q_r \parallel M_r')$  which requires  $U_r$ 's smart card. Moreover,  $S$  is authenticated by  $U_r$  by checking  $\tau_s' = \tau_s$  whereas,  $\tau_s = h(\alpha_r \parallel ID_r \parallel Q_s)$  and it requires server's private key  $ssk$  to extract  $ID_r$  of legal  $U_r$ . Thus, our proposed protocol ensures mutual authentication.

#### 4.1.4 Server and User Impersonation Attack

For authenticating the login request  $\{PID_r, \tau_r, Q_r\}$  and challenge message  $\{PID_r, \tau_r, Q_r\}$ , it is important to know that legal challenge message can only be generated by the legal  $S$  as it includes  $RP_r$  and to calculate it  $PW_r$  is required. On the other hand, only the legal  $S$  can answer to the authentication message via the challenge message  $\{N_s, \tau_s\}$ .

#### 4.1.5 Stolen Verifier and Insider Attack

Our proposed protocol doesn't maintain any table in the database. Moreover,  $S$  also does not maintains any parameter or data related to the  $PW_r$  of  $U_r$ . that may

helps to null and void stolen verifier attack. Also,  $PW_r$  of  $U_r$  is not being exposed because it not sent in the plain text. So, any insider can't misuse the password of  $U_r$ .

#### 4.1.6 Password Guessing Attack

Password  $PW_r$  of  $U_r$  is protected with the random number  $a_r$ . Moreover, the hash is being implemented on the concatenation of the  $PW_r$  and random number  $a_r$ . Further, the smart card is secured in such a way that it doesn't provide any kind of hint of  $U_r$ 's password  $PW_r$  validity. Therefore, it's impossible for an adversary  $A$  to launch this attack in proposed scheme.

#### 4.1.7 Replay Attack

Consider  $A$  can intercepts  $U_r$ 's request message and replays it after some time, but  $A$  will not able to answer the challenge message that comes from  $S$ . As the calculation of  $PID_r$  includes random number that makes it session specific. That's why, on proposed protocol replay attack is not possible.

#### 4.1.8 Perfect Forward Secrecy

$SK$  which is calculated among  $S$  and  $U_r$  encompasses  $Q_r$  and  $Q_s$  consisting of random numbers from both participants reciprocally. Thus, if  $A$  can get previous secret keys of any promoter, still  $A$  will not be able to find that two different sessions are initiated by same user. So, proposed scheme offers perfect forward secrecy.

#### 4.1.9 No Clock Synchronization

No time stamp is used by both participants, user and server, rather they generate their own random numbers. Therefore, precious resources are being saved by avoiding clock synchronization.

## 4.2 Formal Security Analysis

To show that our proposed protocol is protected, we have adopted same analysis mechanism which is mentioned in [33]. For the analysis purpose, below oracles are described:

- **Reveal:** The purpose of this oracle is to output a string  $Z$  through one way hash function as  $Y = h(Z)$ .
- **Extract:** For a given input at a point  $O = kU$  and  $U$  this oracle returns a scalar  $k$ .

**Theorem 1.** Proposed protocol is absolutely protected against an adversary  $A$  for the perseverance of the  $U_r$ 's identity ( $ID_r$ ), secret key ( $ssk$ ) of  $S$ , calculated  $SK$  among  $U_r$  and  $S$  under hard supposition of ECDLP and random oracle protected hash functions.

**Proof 1.** Suppose  $A$  has abilities to extract  $U_r$ 's identity  $ID_r$ ,  $S$ 's private key  $ssk$  and calculates  $SK$ . For this purpose  $A$  performs  $EXPE1_{A, PRUSAS}^{ECDLP, HASH}$  algorithmic

experiment authentication protocol PRUAS against solicited remote-user through simulating oracles Reveal and Extract. We have defined probability achieved of above mentioned analysis as  $Suce_1 = |\Pr b[EXPE1_{A,PRUSAS}^{ECDLP,HASH} = 1] - 1|$ . Benefits taken by adversary A is described as  $\max_A(Suce_1) = A1_{A,TFBAMS}^{HASH,ECDLP}(t_e, q_{ex}, q_{rv})$ ,

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**Algorithm 1.**  $EXPE1_{A,PRUSAS}^{ECDLP,HASH}$ 


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1: Intercept log in message  $\{PID_r, \tau_r, Q_r\}, \tau_r =$ 
    $h(ID_r || \alpha_r || Q_r || M_r), Q_r = q_r \cdot P$ 
2: Call the Reveal on oracle  $\tau_r$  and get
    $h(ID_r || \alpha_r || Q'_r || M_r) \leftarrow \text{Reveal}(\tau_r)$ 
3: Call the Reveal on oracle  $h(ID_r || M_r)'$  and get
    $(ID'_r || M'_r) \leftarrow \text{Reveal}(h(ID_r || M_r)')$ 
4: if  $(M'_r = M_r)$  then
5:   Compute  $\tau'_r = h(ID_r || \alpha_r || Q_r || M'_r)$ 
6:   if  $(\tau_r = \tau'_r)$  then
7:     Accept  $ID'_r$ 
8:     Compute  $ssk' = (ssk \oplus ID'_r) \oplus ID_r$ 
9:     Eavesdrop the challenge message
        $\{N_s, \tau_s\}$ , Where  $N_s = Q_s \oplus M_r$ ,
        $\tau_s = h(\alpha_r || ID_r || Q_s)$ 
10:    Compute  $Q'_s = N_s \oplus M_r$ 
11:    Compute  $\tau'_s = h(\alpha_r || ID_r || Q'_s)$ 
12:    if  $(\tau'_s = \tau_s)$  then
13:      Accept  $ssk$ 
14:      Calculate  $SK = h(ID_r || Q_r || Q_s || M_r)$ 
15:    else
16:      return Fail
17:    end if
18:  else
19:    return Fail
20:  end if
21: else
22:   return Fail
23: end if

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Whereas adversary A can take maximum of  $q_{rv}$  Reveal and  $q_{ex}$  Extract inquiries. According to analysis adversary A can calculate  $ID_r$ ,  $ssk$  and  $SK$  if and only if he can inverse 1 the protected hash function and 1 breach ECDLP. Therefore, cited to the Definition 1, to inverse the protected hash function is infeasible to calculate in polynomial time, as by the Definition 1 to breach ECDLP is impossible to calculate. Thus, we

have  $A1_{A,PRUSAS}^{HASH,ECDLP}(t_e, q_{ex}, q_{rv}) \leq \epsilon$ . Hence, improved authentication of remote user protocol is invulnerable A to calculate  $U_r$ 's  $ID_r$ , S's private key  $ssk$  and calculate  $SK$ .

## 5 Performance and Security Comparisons

This section demonstrates the security and performance analysis of proposed protocol. Performance of the proposed scheme has verified by using following tools which are described as, cryptographic functions used in proposed scheme were implemented using inbuilt PyCrypto library in Ubuntu 19.04, with system specifications, 16.0 GB RAM and 3.60 GHZ processing power with core i7 using python programming language. The proposed protocol was implemented various times under similar conditions to get the average time. The amount of time require for XOR and concatenation is negligible that's why these values are not considered. Moreover, hash operation, point multiplication and point addition takes 0.00093 ms, 0.00037 ms and 0.00028 ms, respectively. Values for identity, password, time stamp, random number, XOR and P are supposed to be 160 bits. Whereas, hash value is considered 256 bits and encryption/decryption, server public key and private key value is considered as 512 bits. The following notations are used to describe computation cost:

$t_h$  time for calculating hash function.

$t_m$  time for calculating the dot product.

$p_a$  time for calculating point addition.

$t_{\oplus}$  time for calculating XOR.

$t_{||}$  time for calculating concatenation.

### 5.1 Cost of Storage

This section describes the storage cost of proposed protocol in comparison of other protocols. Storage cost is basically the storage required for credentials stored in  $SC_r$  and database.

The total storage cost of our protocol is 672. Moreover, cost of storage for Qu and Tan's [31], Huang et al.'s [32] and Chaudhry et al.'s [33] are 928 bits, 672 bits and 928 bits, respectively. Storage cost is described in Table 2 and Figure 4. The number of bits are represented on Y-axis and protocols are represented on X-axis, shown in Figure 4. It demonstrates that the storage cost of proposed protocol is less than [31, 33] and almost equal to [32] protocol.

**Table 2.** Storage cost

Protocols	Storage cost
Qu et al. [31]	928
Huang et al. [32]	672
Chaudhry et al. [33]	928
Proposed	672

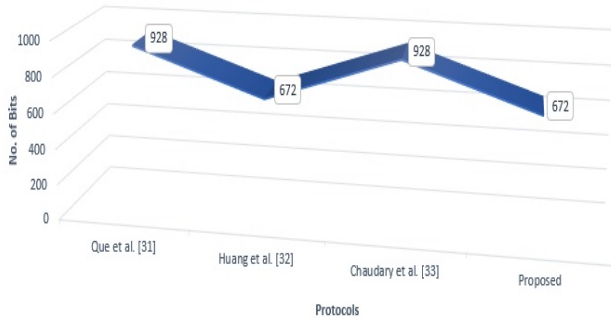


Figure 4. Storage cost comparison

5.2 Cost of Communication

Comparison and analysis of communication cost of the proposed scheme in compare to the other protocols are carried out in this section. Proposed protocol requires 211 bits for communication. Likewise, communication cost of Qu et al.’s, Huang et al.’s and Chaudhry et al.’s protocol are 3392 bits, 3136 bits, 2880 bits, respectively shown in Figure 5 and Table 3. Whereas, Figure 5 states that the communication cost of proposed protocol is less than all related protocols [31-33].

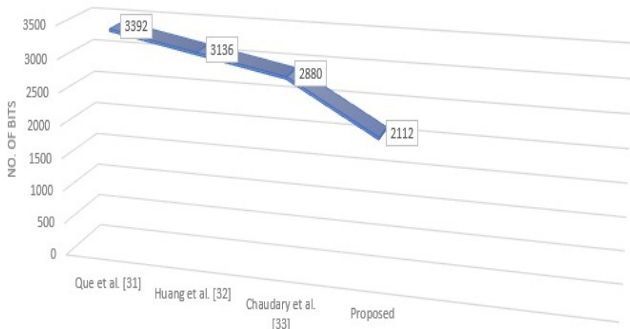


Figure 5. Communication cost comparison

Table 3. Communication cost

Protocols	Cost of Registration (in bits)	Cost of login and Authentication (in bits)	Total Cost (in bits)
Qu and Tan [31]	1184	2208	3392
Huang et al. [32]	928	2208	3136
Chaudhry et al. [33]	928	1952	2880
Proposed	928	1184	2112

5.3 Cost of Computation

In this section, we compare and analyze computation cost of proposed protocol with related protocols shown in Table 4 Proposed protocol carries out, 9 one way hash functions and 4 point of multiplications whereas, the computation cost is calculated in milliseconds(ms).

Table 4. Computation cost

Protocols	Computation Cost	Cost (in ms)
Qu et al. [31]	$9t_m + 5p_a + 13t_h + 2t_{\oplus} + 17t_{\parallel}$	= 0.01679
Huang et al. [32]	$6t_m + 1p_a + 17t_h + 7t_{\oplus} + 24t_{\parallel}$	= 0.01831
Chaudhry et al. [33]	$6t_m + 1p_a + 12t_h + 5t_{\oplus} + 16t_{\parallel}$	= 0.01366
Proposed	$4t_m + 9t_h + 8t_{\oplus} + 17t_{\parallel}$	= 0.00985

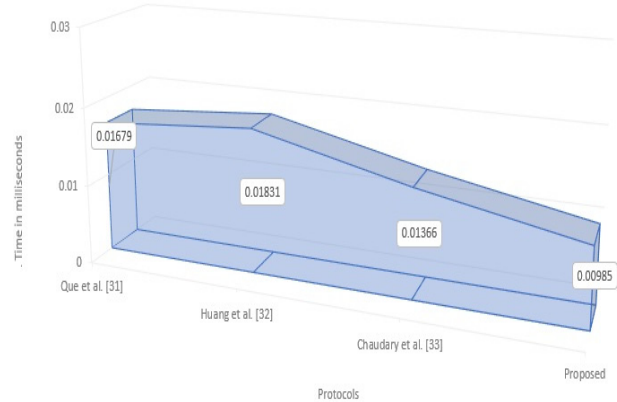


Figure 6. Computation cost comparison

The Figure 6 shows the time required for computation by the related and proposed protocols. The time required in ms is represented on vertical axis whereas, the protocols are represented on horizontal axis.

Whereas P= Provides and NP= Not Provides.

Table 5 shows the comparison of proposed and related protocols in terms of security features. After analyzing Table 3, Table 4 and Table 5 we conclude that the computation, storage and communication cost of proposed protocol is less and provides more security than other protocols.

Table 5. Comparison of security parameters

Protocols	[31]	[32]	[33]	Proposed
Prevents smart card Stolen attack	NP	P	NP	P
Impersonation Attack	NP	NP	P	P
Mutual Authentication	P	P	P	P
Perfect Forward Secrecy	P	P	P	P
Prevents Replay Attack	P	P	P	P
Privacy and Anonymity	P	P	P	P
Prevents Insider and Stolen Verifier Attack	P	P	P	P
Prevents Password Guessing Attack	NP	P	P	P
No Clock Synchronization	P	P	P	P

## 6 Conclusion

In this paper, using ECC, we have presented lightweight remote user authentication protocol. The extensive analysis has proved that all related protocols are costly and were also vulnerable to some major attacks. So, we have presented an enhanced scheme that proves to be more secure. Moreover, our proposed protocol is precisely analyzed through informal and formal analysis of security. Further, the analysis proved that our proposed protocol is more robust and lightweight in comparison of other related protocols. Thus, due to the enhanced performance and security features, our proposed protocol has proved to be more efficient, lightweight and practical.

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